

Stat 242 Quiz – Topics Drawn from Sections 2.3, 5.2, and 6.2

What's Your Name? _____

In the 1970's, it was found that giving terminal cancer patients a dietary supplement of ascorbate could prolong their lives. As a follow-up question, researchers wondered if the effect of the ascorbate was different when different organs were affected by the cancer. We have a data set with records for 64 different cancer patients. Each patient had cancer in one of 5 different organs: breast, bronchus, colon, ovary, or stomach. For each patient, we have recorded their cancer type and their survival time. Here we will treat the log of survival time as the response variable. The R code below calculates the mean log survival time for each group of patients.

```
cancer %>%
  group_by(Organ) %>%
  summarize(
    mean_log_survival_time = mean(Survival)
  )
```

```
## # A tibble: 5 x 2
##   Organ      mean_log_survival_time
##   <chr>          <dbl>
## 1 Breast          1396.
## 2 Bronchus         212.
## 3 Colon           457.
## 4 Ovary           884.
## 5 Stomach         286
```

Define the parameters as follows:

- μ_1 is the mean log survival time for breast cancer patients similar to those enrolled in this study;
- μ_2 is the mean log survival time for bronchus cancer patients similar to those enrolled in this study;
- μ_3 is the mean log survival time for colon cancer patients similar to those enrolled in this study;
- μ_4 is the mean log survival time for ovarian cancer patients similar to those enrolled in this study; and
- μ_5 is the mean log survival time for stomach cancer patients similar to those enrolled in this study

1. We would like to see if the average log survival time for breast cancer is different from the average log survival time for stomach cancer. State the hypotheses for this test as a linear combination of the means for the five groups.

2. Show how you could find an estimate of the linear combination specified in the hypotheses for part 1. (You can just do the set up, no need to simplify to find an actual number.)

(See question 3 on other side!)

3. We would like to see if the average log survival time for breast and ovary cancers (treated as a group) are different from the average log survival time for the other three types. State the hypotheses for this test as a linear combination of the means for the five groups.

For your reference, here are our parameter definitions again:

- μ_1 is the mean log survival time for breast cancer patients similar to those enrolled in this study;
- μ_2 is the mean log survival time for bronchus cancer patients similar to those enrolled in this study;
- μ_3 is the mean log survival time for colon cancer patients similar to those enrolled in this study;
- μ_4 is the mean log survival time for ovarian cancer patients similar to those enrolled in this study; and
- μ_5 is the mean log survival time for stomach cancer patients similar to those enrolled in this study

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The R code below produces output for a confidence interval and a hypothesis test for the hypotheses

$$H_0 : \frac{1}{2}(\mu_1 + \mu_4) - \frac{1}{3}(\mu_2 + \mu_3 + \mu_5) = 0$$

$$H_A : \frac{1}{2}(\mu_1 + \mu_4) - \frac{1}{3}(\mu_2 + \mu_3 + \mu_5) \neq 0$$

Here, the parameters are as follows:

- μ_1 is the mean log survival time for breast cancer patients similar to those enrolled in this study;
- μ_2 is the mean log survival time for bronchus cancer patients similar to those enrolled in this study;
- μ_3 is the mean log survival time for colon cancer patients similar to those enrolled in this study;
- μ_4 is the mean log survival time for ovarian cancer patients similar to those enrolled in this study; and
- μ_5 is the mean log survival time for stomach cancer patients similar to those enrolled in this study

```
anova_fit <- lm(log_survival_time ~ Organ, data = cancer)
fit.contrast(anova_fit, "Organ", c(1/2, -1/3, -1/3, 1/2, -1/3), conf.int = 0.95)
```

```
##      Estimate Std. Error t value Pr(>|t|) lower CI upper CI
## [1,]      1.13      0.351    3.23 0.00204    0.43    1.83
```

(a) Draw a conclusion about the strength of evidence against the null hypothesis. Your statement should be in the context of this question.

(b) Interpret the confidence interval in context. Include a description of the meaning of the phrase “95% confident” as part of your answer.

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The researchers were interested in seeing whether or not the difference in mean log survival times between breast cancer patients and ovarian cancer patients is 0, among patients similar to those enrolled in this study. They expressed this question in the following hypothesis test:

$$H_0 : \mu_1 - \mu_4 = 0$$

$$H_A : \mu_1 - \mu_4 \neq 0$$

Here, μ_1 represented the mean for breast cancer patients and μ_4 represented the mean for ovarian cancer patients.

Based on their sample data, an estimate of $\mu_1 - \mu_4$ was 0.408, with a standard error of 0.607.

(a) Show the set up for calculating a t statistic to use for this test, based on the estimate and standard error above. No need to simplify to get an actual number.

(b) What are the degrees of freedom for the distribution of the t statistic?

(c) Suppose the t statistic above worked out to be 1 (it wouldn't, this is just for illustration). Draw a picture illustrating how the p-value for the test would be calculated.

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In the 1970's, it was found that giving terminal cancer patients a dietary supplement of ascorbate could prolong their lives. As a follow-up question, researchers wondered if the effect of the ascorbate was different when different organs were affected by the cancer. We have a data set with records for 64 different cancer patients. Each patient had cancer in one of 5 different organs: breast, bronchus, colon, ovary, or stomach. For each patient, we have recorded their cancer type and their survival time. Here we will treat the log of survival time as the response variable.

The researchers were interested in the difference in mean log survival times between breast cancer patients and ovarian cancer patients, among patients similar to those enrolled in this study. They expressed this difference as $\mu_1 - \mu_4$, where μ_1 represented the mean for breast cancer patients and μ_4 represented the mean for ovarian cancer patients.

Based on their sample data, an estimate of $\mu_1 - \mu_4$ was 0.408, with a standard error of 0.607.

Use the R output below to answer the following question.

```
qt(0.975, df = 64)
```

```
## [1] 1.99773
```

```
qt(0.975, df = 63)
```

```
## [1] 1.998341
```

```
qt(0.975, df = 62)
```

```
## [1] 1.998972
```

```
qt(0.975, df = 59)
```

```
## [1] 2.000995
```

(a) What is the degrees of freedom for the t statistic?

(b) Show the set up for calculating a 95% confidence interval for $\mu_1 - \mu_4$, based on the estimate and standard error above. No need to simplify to get numbers, just show the set up. You will need the output from just one of the calls to qt above.

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The researchers were interested in whether there was a difference in mean log survival times between breast cancer patients and ovarian cancer patients, among patients similar to those enrolled in this study.

Use the R output below to answer the following questions.

```
anova_fit <- lm(log_survival_time ~ Organ, data = cancer)
summary(anova_fit)

##
## Call:
## lm(formula = log_survival_time ~ Organ, data = cancer)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.3805 -0.6607  0.1025  0.8207  2.0460
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    6.5586     0.3603  18.201 < 2e-16 ***
## OrganBronchus -1.6054     0.4625  -3.472 0.000975 ***
## OrganColon    -0.8095     0.4625  -1.750 0.085247 .
## OrganOvary    -0.4080     0.6065  -0.673 0.503801
## OrganStomach -1.5907     0.4896  -3.249 0.001915 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.195 on 59 degrees of freedom
## Multiple R-squared:  0.2252, Adjusted R-squared:  0.1726
## F-statistic: 4.286 on 4 and 59 DF,  p-value: 0.004122
```

(a) What is an estimate of the difference in mean log survival times for breast cancer and ovarian cancer patients?

(b) State the null and alternative hypotheses for a relevant hypothesis test in terms of one of the model parameters β_0 , β_1 , β_2 , β_3 , or β_4 .

(See question c on other side!)

(c) What is the p-value for the test? State a conclusion for the test in terms of strength of evidence against the null hypothesis.

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The researchers fit an ANOVA model to these data with log survival time as the response and the affected organ as the explanatory variable.

Use the R output below to answer the following questions.

```
anova_fit <- lm(log_survival_time ~ Organ, data = cancer)
summary(anova_fit)

##
## Call:
## lm(formula = log_survival_time ~ Organ, data = cancer)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.3805 -0.6607  0.1025  0.8207  2.0460
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    6.5586     0.3603  18.201 < 2e-16 ***
## OrganBronchus -1.6054     0.4625  -3.472 0.000975 ***
## OrganColon    -0.8095     0.4625  -1.750 0.085247 .
## OrganOvary    -0.4080     0.6065  -0.673 0.503801
## OrganStomach  -1.5907     0.4896  -3.249 0.001915 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.195 on 59 degrees of freedom
## Multiple R-squared:  0.2252, Adjusted R-squared:  0.1726
## F-statistic: 4.286 on 4 and 59 DF,  p-value: 0.004122
```

(a) Write down the linear model equation for the population mean log survival time as a function of the model parameters β_0 , β_1 , β_2 , β_3 , and β_4 .

(b) In the background, R created a new variable called `OrganStomach`. Explain what that variable is (what are the possible values for that variable, and when does it take each of those values?).

(See questions c through f on other side!)

(c) Write down the population mean log survival time for patients who have breast cancer in terms of the model parameters β_0 , β_1 , β_2 , β_3 , and β_4 .

(d) Write down the population mean log survival time for patients who have ovarian cancer in terms of the model parameters β_0 , β_1 , β_2 , β_3 , and β_4 .

(e) What is the interpretation of β_0 ?

(f) What is the interpretation β_3 ?